# Discussion Problems for Math 180 

Thursday, October 16

1. (a) Express $\frac{1}{2} \ln (y)-2 \ln (x)+1$ as a single logarithm.
(b) Sketch a graph of $\frac{1}{2} \ln (y)-2 \ln (x)+1=0$.
2. Consider taking a number to its own power: for instance, $1^{1}=1$ and $2^{2}=4$, while

$$
\left(\frac{1}{2}\right)^{1 / 2}=\frac{1}{\sqrt{2}} \approx 0.7071
$$

and so on. Which positive number, taken to its own power, gives the smallest result?
3. Give an example of a function with domain $(-\infty, \infty)$ that has no local minima or maxima.
4. (a) Write down the equation for a circle of radius $r$ centered at $(h, k)$.
(b) A circle passes through the point $(7,0)$ and is tangent to the line $3 x+4 y=31$ at the point $(5,4)$. What are the center and radius of this circle?
5. Give an example of a polynomial function which has a local max at $(0,1)$ and a local min at $(2,0)$.

